How Big Are Those Shoes?

Assessment Type	**Recommended Grade Level**	**MYP Criterion Level**
Real-life Application of Mathematics	Grade 9 (MYP4) Extended	MYP 5

MYP Assessment Criteria
Criterion D: Applying mathematics in real-life contexts

MYP Command Terms Used
identify, apply, find, describe, select, apply, discuss, suggest, explain, justify, use,

MYP Global Context
Orientation in space and time

MYP Key Concepts
Form

MYP Related Concepts
Space, Models, Representation

MYP Branch of Mathematics
Numerical and abstract reasoning

MYP Topics and Skills

- Number operations
- Operating with algebraic expressions
- Substitution into expressions
- Expanding brackets

Prior Knowledge Needed

- Writing mathematical expressions in one variable
- Multiplying binomial by binomial
- Combining like terms to simplify polynomial expressions
- Substitute values into polynomials

Assessment Description

In this assessment, students are presented with a scenario that involves using a variable to represent the length of different wall sections in a room that needs to be painted. As students work through the scenario following logical steps in their calculations, they describe their steps, suggest corrections to given estimates, identify polynomial expressions, calculate lengths and areas, and explain/justify the degree of accuracy used and whether the findings make sense. By the end of the task, students find and justify the possible value of the initial variable.

Materials Needed

The use of a scientific calculator is required. The use of a graphic display calculator is not necessary but allowed.

Task-specific instructions / Recommendations

Students are advised to read questions carefully and consider the hints/tips provided in the various speech bubbles.

Assessment Criterion D: *Applying mathematics in real-life contexts*

	Achievement Level Descriptor (MYP5)	Task Specific Descriptor
0	The student **does not** reach a standard described by any of the descriptors below.	
1-2	The student is able to: i. identify **some** of the elements of the authentic real-life situation ii. apply mathematical strategies to **find a solution** to the authentic real-life situation, **with limited success** iii. *(not demonstrated at this level)* iv. *(not demonstrated at this level)* v. *(not demonstrated at this level)*.	The student is able to: i. **identify** the mathematical expressions that represent the measured walls (Q1) ii. **apply** the appropriate mathematical operations to **find** the required expressions and briefly **describe** the steps taken (Q2) iii. *(not demonstrated at this level)* iv. *(not demonstrated at this level)* v. *(not demonstrated at this level).*
3-4	The student is able to: i. identify the **relevant** elements of the authentic real-life situation ii. select, **with some success, adequate** mathematical strategies to model the authentic real-life situation iii. apply mathematical strategies to **reach a solution** to the authentic real-life situation iv. *(not demonstrated at this level)* v. **discuss** whether the solution makes sense in the context of the authentic real-life situation.	The student is able to: i. **identify** the missing mathematical expression and briefly **describe** what each of the three expressions in the floor's area represent (Q3) ii. **select** the appropriate method and briefly **describe** the steps taken (Q4) iii. **apply** the appropriate method(s) to **find** the required expression in the simplest form (Q4) iv. *(not demonstrated at this level)* v. **discuss** the error in Scott's estimation and **suggest** a correction (Q5)
5-6	The student is able to: i. identify the **relevant** elements of the authentic real-life situation ii. select **adequate** mathematical strategies to model the authentic real-life situation iii. apply the selected mathematical strategies to **reach a valid solution** to the authentic real-life situation iv. **explain** the degree of accuracy of the solution v. **explain** whether the solution makes sense in the context of the authentic real-life situation.	The student is able to: i. **identify** the wall whose paintable area is represented by the given expressions (Q6) ii. **select** the appropriate method(s) to find the required values (Q7) iii. **apply** the appropriate method(s) to **find** the required values (Q7) iv. **find** a reasonable range and **explain** the degree of accuracy in Scott's estimation (Q8) v. **explain** whether Scott's estimate makes sense for the total paintable area (Q8)
7-8	The student is able to: i. identify the **relevant** elements of the authentic real-life situation ii. select **appropriate** mathematical strategies to model the authentic real-life situation iii. apply the selected mathematical strategies to **reach a correct solution** to the authentic real-life situation iv. **justify** the degree of accuracy of the solution v. **justify** whether the solution makes sense in the context of the authentic real-life situation.	The student is able to: i. **identify** the number of medium and small cans of paint Scott must have used (Q9) ii. **select** the appropriate method(s) to find the required values and **describe** each step taken (Q10) iii. **apply** the appropriate method(s) to **find** the length of Scott's shoes (Q10) iv. **suggest** the US shoe size that Scott wore and briefly **explain** and **justify** why they think so (Q11) v. **use** the suggested shoe size to **find** the required values and **justify** whether those values make sense (Q12)

Scattered Scott was a painter, and he was notorious for forgetting to carry his tools. His name, *Scattered Scott*, was a nickname he earned over time after other painters learned that he constantly forgot his tools.

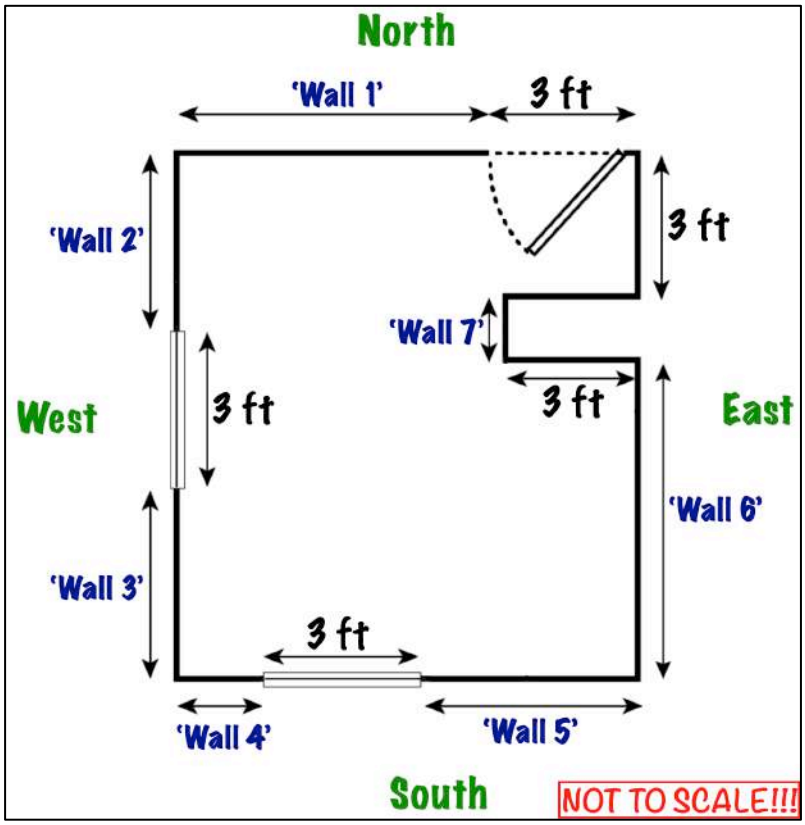
In this assessment task, we explore his method to make reasonable measurements for his job: painting walls. How does he do it? What other tools does he use? How accurate are his methods?

Let's explore!

In his last paint job, once again, staying true to his nickname, Scott did not have his measuring tools. Luckily, he remembered some of the measurements he was told:

- The door was exactly 3 feet wide and 7 feet tall.
- The windows were square-shaped, each measuring 3 feet by 3 feet.
- One of the sides of the small wall on the East side was 3 feet wide.
- The ceiling-to-floor height was exactly 8 feet.

He quickly sketched a floor plan, marked these measurements, and labeled all other sections of the walls from *Wall 1* to *Wall 7*. He then wrote "NOT TO SCALE!!!" in the corner of his sketch.



Not having proper measuring tools, Scott decided to use *his shoes* to measure the length of some wall sections. His measurements were the following:

- *Wall 1*: about 1/3 of a shoe length longer than 22 shoe lengths,
- *Wall 2* and *Wall 3*: each 13 shoe lengths (a tiny bit shorter, but nearly exactly),
- *Wall 4*: about 3/4 of a shoe length more than 3 shoe lengths (maybe a bit less),
- *Wall 7*: a few centimeters shorter than 2 shoe lengths.

Let's see how we can work with these measurements!

Let S represent the length of Scott's shoe, in feet, used in the measurements.

(1) Ignoring the minor inaccuracies, **identify** mathematical expressions in terms of S to represent the measured walls.

Wall 1	Wall 2	Wall 3	Wall 4	Wall 7

[D: 1-2, i]

Scott did not measure all wall sections as he knew he could use what he measured to figure out the rest of the lengths.

(2) **Apply** the appropriate mathematical operations to **find** mathematical expressions in terms of S to represent the length of

a. Wall 5 and Wall 6,
b. the Northern wall, and
c. the Western wall.

For each wall, briefly **describe** the step(s) taken to find the length.

[D: 1-2, ii]

Scott wrote down an *incomplete* expression to represent the room's floor area:

(3) **Identify** the missing mathematical expression below.

Floor's Area: $\left(22\frac{1}{3}S + 3\right)(26S + 3) -$ ☐

Briefly **describe** what each of the three expressions in the floor's area represents.

[D: 3-4, i]

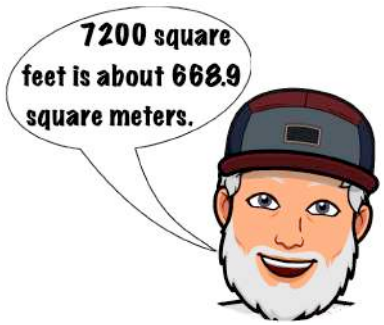
(4) **Select** and **apply** the appropriate method(s) to **find** the expression for the floor's area in the simplest form. Briefly **describe** the steps taken.

[D: 3-4, ii-iii]

Scott decided to make a rough estimation, so he said to himself:

> *"If my shoes are about 10 inches, then the floor area is about* $580 \times 100 + 139 \times 10 + 10$ *or* $(580 + 139 + 1)(10) = (720)(10) = 7200$ *square feet. This is about 670 square meters."*

(5) Briefly **discuss** the error in Scott's estimation and **suggest** a correction that would provide a more reasonable estimation.
(Note: 1 in. = 2.54 cm and 1 ft. = 12 in.)



[D: 3-4, v]

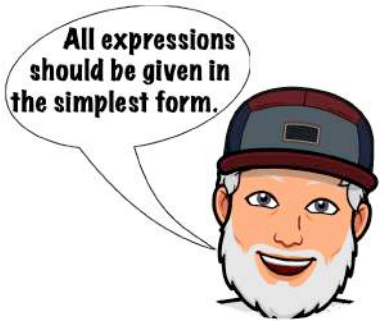
As all four walls needed to be painted, Scott found a mathematical expression, in terms of his shoe size S, for each wall. Expressions for two of the four walls are given below.

(6) **Identify** the wall whose *paintable area* is represented by the given expressions.

$(26S + 3)(8) - (3)(3)$	$\left(22\frac{1}{3}S + 3\right)(8) - (3)(7)$
Wall:	Wall:

[D: 5-6, i]

(7) **Select** and **apply** the appropriate method(s) to **find**
   a. the simplest form of each expression given in question (6),
   b. a mathematical expression in terms of S for
      i. the *paintable area* of the other two walls,
      ii. the *total paintable wall* area.

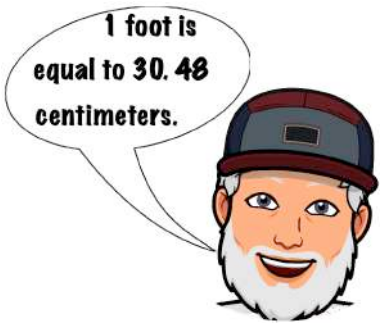


*Remember: S represent Scott's shoe size **in feet**!*

[D: 5-6, ii-iii]

Scott decided to make another rough estimation:

"I've painted rooms like this before, and I think the total paintable area is about 75 square meters!"



(8) Given that Scott's shoe size is between 25 and 30 centimeters, **find** a reasonable range for the total paintable area.

Then, **explain** the degree of accuracy in Scott's estimation and whether his estimate makes sense for the total paintable area.

[D: 5-6, iv-v]

When Scott checked his truck, he found several brand-new cans of paint:

- large cans, each advertised to cover an area of 12 square meters,
- median cans, each advertised to cover an area of 7 square meters, and
- small cans, each advertised to cover an area of 4 square meters.

After painting one coat of paint covering the total paintable area, Scott thought to himself:

"If those stickers on the cans are true,
I painted exactly 74 square meters."

(9) Given that Scott used 4 large cans of paint and a combination of medium and small cans, **identify** the number of medium and small cans of paint he must have used (without having any leftover paint).

[D: 7-8, i]

Given that Scott in fact painted exactly 74 m^2,
it's time to find out how big Scott shoes are!

(10) **Select** and **apply** the appropriate method(s) to **find** the length of Scott's shoes in feet, in inches, and in centimeters. **Describe** each step of your strategy in detail.

[D: 7-8, ii-iii]

A guide for men's shoe sizes is shown on the right, from this source.

MEN'S SHOES SIZE GUIDE
(CHART FOR SHOES MEASUREMENT)

US	UK	EU	CM	IN
7	6	40	25.4	10
7.5	6.5	41	25.8	10 1/8
8	7	41-42	26	10 1/4
8.5	7.5	42	26.7	10 1/2
9	8	43	27.3	10 3/4
9.5	8.5	43-44	27.7	10 7/8
10	9	44	27.9	11
10.5	9.5	44-45	28.6	11 1/4
11	10	45	29.2	11 1/2

(11) Based on your findings in the previous question(s), **suggest** the US shoe size that Scott was wearing when taking the measurements.

Briefly **explain** why you think so, **justifying** the degree of accuracy in your suggestion.

[D: 7-8, iv]

(12) **Use** the shoe size you suggested in question (11) that Scott was wearing when measuring the wall sections to **find**

a. the length of the northern and western walls in feet, inches, and centimeters, and
b. the floor area in square feet, square inches, and square meters.

Then, based on your findings, **justify** whether those values make sense.

And now we know Scattered Scott shoe size! Well done!

[D: 7-8, iv]